1. A poster is to contain 50 square inches of printed matter with margins of 4 inches at both the top and the bottom and 2 inches at each side. Find the dimensions that will minimize the total area of the poster.

2. A rectangular, open-top box is to be made from a piece of cardboard 24 inches long and 9 inches wide by cutting out identical squares from the corners and turning up the cardboard to form the sides. Find the maximum volume of the box.

3. A homeowner wishes to erect a fence enclosing a rectangular area adjacent to a barn which is 20 feet long. The diagram below illustrates his plan for the fenced area. Find the largest area that can be enclosed if 96 feet of fencing material is available.
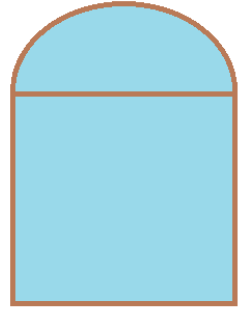
4. An arch top window is being built whose bottom is a rectangle and the top is a semicircle. If there is 12 meters of framing materials, find the width of the window that lets in the most light (largest area).

5. Let $f(x) = 12x^{\frac{2}{3}} - 4x$

a) Find the intervals on which f is increasing. Justify your answer.

b) Find the x-coordinates of all relative maximum and minimum points. Justify your answer.

c) Find the intervals on which f is concave down. Justify your answer.